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Information, Market Incentives, and Student Performance

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ABSTRACT

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This paper uses a discontinuity on the test score disclosure rules of the National Secondary Education Examination in Brazil to test whether test score disclosure affects student performance, the composition of students in schools, and school observable inputs. We find that test score disclosure has a heterogeneous impact on test scores, but only increases average test scores in private schools. Since test score disclosure has no impact on student composition and school observable inputs in both public and private schools, our results suggest that test score disclosure changes the behavior of teachers and school managers in private schools by affecting the market incentives faced by such schools. We also develop a model of school and student behavior to help explain our empirical findings.

JEL Classification: 120, 121

test score disclosure, market incentives, public and private schools Keywords:

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1 Introduction

The literature that studies the effect of school accountability on student performance is by now large. There are two ways in which school accountability can have an impact on student performance. First, to the extent that information about student performance provides information about school quality, school accountability allows school actors to make better informed decisions. For instance, parents can choose schools and students can adjust their effort based on information about test scores. Second, a school accountability system that ties rewards and punishments to test scores directly affects the incentives faced by teachers and school managers.

An important question is whether the disclosure of information about student performance is enough to influence the behavior of teachers and school managers or one needs to provide direct, explicit, incentives to these agents by tying pay to student performance. Test score disclosure by itself can have an impact on the behavior of teachers and school managers if this disclosure affects the (implicit) market incentives faced by schools. The disclosure of information about student performance affects the market incentives faced by schools when school revenues depend on (market) perceptions about school quality, in which case teachers and school managers can react to test score disclosure even in the absence of an explicit link between pay and student performance.

In this paper, we take advantage of a discontinuity on the test score disclosure rules of the National Secondary Education Exam (ENEM) in Brazil to test whether test score disclosure affects the market incentives faced by schools in the São Paulo metropolitan area.³ The ENEM was created in 1998 by the Brazilian Ministry of Education to assess the proficiency of high school graduates in the country. In 2006 the Ministry of Education established that starting with the 2005 ENEM, schools with 10 or more ENEM takers in a year would have their average ENEM score in the year publicly released.

We use a regression discontinuity design to estimate the impact of the disclosure of the average 2005 ENEM scores on: (i) the performance of students in the 2007 ENEM; (ii) the composition of

¹See Figlio and Loeb [2011] for a comprehensive survey.

²It is not consensual that test scores provide a clear signal of school quality. Mizala et al. [2007] shows that in Chile average test scores are very volatile and highly correlated with students' socioeconomic status.

³The São Paulo metropolitan area is the largest metropolitan area in Brazil, with close to 20 million inhabitants.

students in schools in 2007; and (*iii*) the school observable inputs in 2007. Our results indicate that in the 2007 ENEM the treated private schools on average outperformed the control private schools by 0.2 to 0.7 standard deviations of the private schools' test score distribution.⁴ The treated public schools did not outperform the control public schools in the 2007 ENEM, though. We also do not find evidence that treated schools, whether public or private, adjusted their observable inputs from 2005 to 2007, or that there were significant changes in the composition of students in treated schools over the same period of time. Finally, we find heterogeneous effects on 2007 ENEM scores among the treated schools. Treated private schools that had average 2005 ENEM scores below the median average score of the private schools presented better results in 2007 than the control private schools that had average 2005 ENEM scores in the same group. On the other hand, treated public schools that had average 2005 ENEM scores above the median average score of the public schools presented worse results in 2007 than the control public schools that had average 2005 ENEM scores above the median average score of the public schools presented worse results in 2007 than the control public schools that had average 2005 ENEM scores in the same group.⁵

Taken together, our empirical results provide evidence that test score disclosure affects the market incentives faced by private schools. Indeed, the fact that test score disclosure does not seem to affect either the composition of students or the observable inputs in treated schools suggests that test score disclosure acts by changing the behavior of students, teachers, and school managers in treated schools. Since teachers and managers in Brazilian public schools have job stability and their earnings are not related to student performance, market incentives should be stronger in private schools.⁶ Moreover, the ENEM is disassociated from any hard accountability policies in Brazil.⁷ Hence, the only channel through which the disclosure of average ENEM scores can have an impact on the behavior of teachers and school managers is by affecting the market incentives

⁴We refer to the schools that had their average 2005 ENEM scores released in 2006 as the treated schools.

⁵The disclosure of the average 2005 ENEM scores took place in February of 2006, roughly 6 months before the 2006 ENEM, when it was probably too late for the disclosure to have an impact on student performance in 2006. In order to check for this possibility, we ran all our regressions for the effect of test score disclosure on student performance using the 2006 sample instead of the 2007 sample and found no statistically significant results.

⁶The wages in Brazilian public schools are set by the government and vary exclusively with tenure and schooling level. The lack of market incentives in public schools is not exclusive to Brazil. Podgursky and Springer [2011] discuss how in the U.S. the public school system is, in general, lacking in market incentives.

⁷In 2008, and so after the period we analyze, the state of São Paulo announced and implemented performance-based payments for teachers and principals in state schools. The payments depend on the schools' average test scores in the SARESP proficiency exam. The SARESP exam is mandatory for students in the 5th, 9th, and 12th grades but a student's score has no direct consequence for the student. Students in private schools do not take the exam.

faced by their schools. Consequently, a difference in the impact of test score disclosure on average test scores between public and private schools indicates that test score disclosure has an effect on the market incentives faced by private schools.

The heterogeneous impact of test score disclosure on test scores shows that it is not obvious a priori how test score disclosure should affect average test scores. Moreover, the fact that public schools face weaker market incentives implies that students in public schools should react differently to test score disclosure than students in private schools, and this can partly offset the impact of the weaker reaction of public schools to test score disclosure. In order to address these issues, in this paper we also develop a formal model of school and student behavior in which public and private schools only differ in terms of the market incentives they face to help explain our empirical findings. Namely, that test score disclosure can have a heterogeneous impact on test scores in both public and private schools but only increase average test scores in private schools.

The rest of the paper is organized as follows. The remainder of the Introduction discusses the related literature. Section 2 discusses the ENEM in more detail. Section 3 describes our data and presents some descriptive statistics. Section 4 discusses our identification strategy. Section 5 presents and discusses our empirical results. Section 6 presents our model of school and student behavior and discusses how the model can explain our empirical findings. Section 7 concludes. The Appendix contains omitted details and proofs.

Related Literature

The literature has found evidence that test score disclosure influences perceptions about school quality and can thus affect school revenues. For instance, Black [1999], Figlio and Lucas [2004], and Fack and Grenet [2010] find that school test score reports affect housing prices. Hastings and Weinstein [2008] find for schools in the Charlotte-Mecklenburg public school district in the US that the fraction of parents choosing higher-performing schools increases after information on school test scores becomes available. Machin and Salvanes [2010] find that in Oslo, allowing parents greater freedom in choosing schools affects housing prices. Koning and van der Wiel [2013] find for schools in the Netherlands that a drop in a publicly available ranking of school quality is correlated with a decrease in the number of entering students. Figlio and Kenny [2009]

find that private contributions to schools in Florida are responsive to school grades.8

Our paper belongs to the literature that studies the impact of information disclosure on student performance. Unlike the literature that investigates the impact of hard accountability systems on student performance, we are able to analyze the informational effect of test score disclosure on student performance; hard accountability systems not only change the information available to the school actors, but also directly affect the incentives faced by teachers and school managers.⁹

The papers most closely related to ours are Andrabi et al. [2009] and Koning and Wiel [2012]. Koning and Wiel [2012] find that in the Netherlands, average grades go up in schools that are poorly evaluated in a national newspaper ranking. Koning and Wiel [2012] do not distinguish between public and private schools, though, and thus cannot evaluate the impact of test score disclosure on the market incentives face by schools. Andrabi et al. [2009] study the impact of releasing to parents report cards with student and school academic performance in Pakistan. They find similar results to us. In particular, they find that the impact of test score disclosure on student performance is much larger in private schools than in public schools. An important difference between Andrabi et al. [2009] our work is that while the release of report cards provides information about student ability and school quality at the same time, the disclosure of the average ENEM scores from a previous cohort of ENEM takers only provides information about school quality.

Finally, our paper is also related to the literature that studies how the disclosure of information about the quality of public schools affects incentives in the public sector. Hussain [2009] shows that disclosing school quality ratings affects the future wages of school principals in England. However, unlike in Brazil, public schools in England have a governing board responsible for hiring and setting principals' wages. Firpo et al. [2012] find that the re-election probability of mayors in Brazil depends on how the schools under their administration—municipalities in Brazil are responsible for the public primary schools—are ranked according to a newly created index to assess the quality of primary public schools.

⁸On the other hand, Mizala and Urquiola [2009] find no consistent effect on the enrollment, tuition, and socioeconomic characteristics of students in Chilean schools that are identified as being outstanding.

⁹There is a substantial literature that studies the impact of hard accountability systems on student performance. See, e.g., Hanushek and Raymond [2005], Dee and Jacob [2009], Bacolod et al. [2009], Chiang [2009], Rockoff and Turner [2010], and Muralidharan and Sundararaman [2011].

2 Institutional Background: ENEM

The ENEM is a non-mandatory exam organized by the National Institute of Educational Studies and Research (INEP), which is part of the Brazilian Ministry of Education (MEC). Until 2008, the ENEM was a one-day exam consisting of 63 multiple-choice questions covering four different subjects and an essay, and its scores were in a 0 to 100 scale standardized to have a mean of 50.¹⁰ Only graduating high school students, that is, those students enrolled in the last grade of high school, and students who have already graduated from high school can take the ENEM.

The number of universities in Brazil (public and private) that use the ENEM as an admission exam has increased substantially since its creation and by now the ENEM is commonly used in the admission process of universities.¹¹ The ENEM is also used to select the beneficiaries of the Federal College Voucher Program (ProUni).

The fact that the ENEM is non-mandatory may raise questions about the selectivity of our sample. In this regard, we should note that the number of graduating high school students taking the ENEM has greatly increased over time. From 2001 to 2008, the take-up rate in the São Paulo metropolitan area increased from 26.1% to 70.9% in public schools and from 29.1% to 87.8% in private schools.¹²

A school's average ENEM score is computed using only the ENEM score of its graduating students, that is, the ENEM scores of students from a given school who have already graduated do not count towards the school's average ENEM score. Moreover, for the purpose of determining whether a school's average ENEM score is publicized, the number of takers in the school is given by its graduating students only. So, for example, a school that has 20 takers but only 9 of them are graduating from high school in that year does not have its average ENEM score disclosed.

School average ENEM scores are available at the INEP's website. Figure 1 shows how average ENEM scores by school appear at the INEP's website.¹³ Although the INEP's website does not

 $^{^{10}}$ After 2008, the ENEM became a two-day exam consisting of 180 multiple-choice questions and an essay, with its scores determined using Item Response Theory.

¹¹The number of students admitted to universities based on their ENEM score was 741,013 in 2006.

 $^{^{12}}$ Over the same period of time, the take-up rate in the whole country increased from 31.4% to 61.8% in public schools and from 25.21% to 72% in private schools.

¹³http://sistemasenem4.inep.gov.br/enemMediasEscola.

contain a ranking of schools based on their average ENEM scores, several newspapers in Brazil produce local, regional, and national rankings. Figure 2 shows a newspaper ranking from a major newspaper in Brazil that circulates in the state of São Paulo. Despite the fact that there is no hard accountability system based on school average ENEM scores, managers, professors, parents, and students care about their schools' average ENEM scores. For instance, real state websites inform the average ENEM score of the schools near a given location. Also, many private schools advertise their average ENEM score on the media and in their websites.

[Insert Figures 1 and 2 around here]

3 Data

We use the 2005 and 2007 ENEM micro databases and the 2005 and 2007 School Census. The ENEM databases have information on students' test scores and schools, as well as information on students' socioeconomic characteristics such as age, race, and family income, among others. The School Census has information on school observable inputs such as student-to-teacher ratio and teachers' and managers' schooling, among others.

Using the ENEM micro database, we can calculate the number of takers for each school in a given year. Therefore, we are able to recover individual ENEM scores for schools below and above the cutoff point of 10 exam takers. Since we have access to individual results, we can calculate school average scores. The ENEM micro databases only became available in 2010, so in 2007 students, teachers, and managers in schools with fewer than 10 exam takers had no access to their schools' average ENEM scores in 2005.

Tables 1 and 2 report some descriptive statistics for both public and private schools. First, as expected, students enrolled in larger private schools have higher scores and better socio-demographic characteristics than students enrolled in smaller private schools. However, larger private schools do not present better observable inputs than the smaller private schools. This first view of the data suggests that for private schools, size maybe correlated with student composition, but not necessarily with school observable inputs. For public schools, the pattern seems to be the opposite, though.

¹⁴See www.zap.com.br, for example.

In the one hand, there is no clear association between school size and student composition. On the other hand, the data suggests that larger public schools are better equipped than smaller ones.

Finally, as expected, we find large differences between private and public schools in Brazil. On average, students in private schools have better socio-demographic characteristics and private schools have better observable inputs.¹⁵

[Insert Tables 1 and 2 around here]

4 Empirical Strategy

We take advantage of the exogenous test score disclosure rule for the 2005 ENEM to estimate the reduced-form causal effects of test score disclosure on: (*i*) the composition of students in schools in 2007; (*ii*) the school observable inputs in 2007; and (*iii*) the 2007 ENEM scores. We also investigate whether test score disclosure has a heterogeneous impact on student performance by analyzing the effect of test score disclosure on the 2007 ENEM scores for two different sets of schools, the set of schools with average 2005 ENEM scores above the median (average score) and the set of schools with average 2005 ENEM scores below the median. In order to investigate the impact of test score disclosure on the market incentives of schools, we work with public and private schools separately.

Consider the following specification:

$$Y_{is} = \alpha_Y + \beta_Y \cdot d_s + \phi_Y(T2005_s - 10) + d_s \cdot \psi_Y(T2005_s - 10) + \varepsilon_{Y,is}, \tag{1}$$

where $T2005_s$ is the number of graduating students taking the ENEM in 2005 in school s and $d_s=1$ if, and only if, $T2005_s$ is at least 10. For a given outcome variable of interest Y in 2007, we are interested in the impact on Y of the publication of the average 2005 ENEM score. The functions ϕ_Y and ψ_Y are flexible functions of the running variable. We consider several different specifications for ϕ_Y and ψ_Y , from non-parametric ones (local linear regressions) to higher-order

¹⁵Although the tables do not allow for a comparison of test scores between private and public schools, since test scores are standardized within each group of schools, the raw data shows that, on average, the test scores of students from private schools are almost one standard deviation above the test scores of students from public schools.

polynomials. The variable $\varepsilon_{Y,is}$ is an unobservable term that is mean-independent of d at T2005 = 10 under usual assumptions on the continuity of ϕ_Y and ψ_Y at T2005 = 10. The coefficient β_Y measures the impact of test score disclosure on Y. We run the regressions at the student level (i) and cluster the standard errors at the school level (s).

It is possible that any observable differences we find in 2007 between schools in the treated and control groups are due to the fact that schools in these two groups face different probabilities of having their average 2007 ENEM scores released. In Section 6, when we present our model of school and student behavior, we discuss how different probabilities of test score disclosure in 2007 could affect the behavior of teachers and schools managers, leading to changes in effort and school observable inputs. However, the relevant group of schools in our sample are the schools close to the treatment discontinuity.¹⁷ As such, it is unlikely that managers and teachers in schools where slightly less than 10 graduating students took the ENEM in 2005 and managers and teachers in schools where slightly more than 10 graduating students took the ENEM in 2005 would (on average) face different probabilities of test score disclosure in 2007. Thus, it seems reasonable to conjecture that any differences we find between treated and control schools comes from the informational shock associated with test score disclosure.

There two important conditions for the validity of the regression discontinuity design (RDD). First, that there is no manipulation of the running variable. Second, that there are no pre-existing systematic differences between schools above and below the treatment discontinuity. If either of these conditions are not met, then we cannot assign to the disclosure of test scores a causal impact on the outcome variables of interest; there would be confounding factors affecting the outcome variables beyond test score disclosure.

We check the validity of the RDD by: (i) observing whether there are jumps in the histogram of the running variable around the cutoff point of 10 ENEM takers; and (ii) using the 2005 ENEM results, the composition of students in schools in 2005, and the school observable inputs in 2005 as outcome variables to see if there are any significant pre-existing differences between schools

¹⁶See Hahn et al. [2001], Imbens and Lemieux [2008], and Lee and Lemieux [2010] for a discussion of the regression discontinuity design methodology.

¹⁷There are 436 schools close to the treatment discontinuity (with 1 to 19 ENEM takers). Out of those schools, 103 are public and 333 are private.

above and below the treatment discontinuity. A jump in the histogram of the running variable around the cutoff point of 10 ENEM takers would indicate that either students or schools were able manipulate test score disclosure in 2005. In this case, any systematic difference between schools above and below the treatment discontinuity could be attributed to unobserved factors correlated with the decision to have test scores disclosed in 2005. Significant pre-existing differences between schools above and below the treatment discontinuity would imply that test score disclosure is not the causal factor explaining the differences in the outcomes variables observed in 2007.

Notice that even if the conditions for the validity of the RRD hold, this does not necessarily mean that test score disclosure is the main mechanism explaining the differences in the outcome variables observed in 2007. For instance, it is possible that any difference in 2007 ENEM scores between schools above and below the treatment discontinuity happens by chance. To discard this possibility, we run specification (1) using several false cutoff points as placebo tests.

5 Data Analysis

In this section, we first check the impact of test score disclosure on student composition, school observable inputs, and average test scores. We then check how the effect of test score disclosure on test scores depends on whether a school's average 2005 ENEM score is above or below the median. Finally, we check the validity of the RDD and the robustness of our results.

5.1 Student Composition and School Observable Inputs

Table 3 shows our estimates for differences in the characteristics of the 2007 ENEM takers between treated and control groups for both types of schools (public or private). We consider the following student characteristics: gender, average age, race, parental education, and family income. The first three columns of the table show the results for private schools, while the last three columns show the results for public schools. We report the results for local linear regressions and second-order polynomial regressions.¹⁸

¹⁸As suggested by Fan and Gijbels [1996] and Imbens and Lemieux [2008], we use triangular kernels and optimal bandwidth for the local linear regressions. The results for other specifications corroborate our main findings and are available upon request.

We find that there are no consistently significant differences in student composition for both types of schools. For private schools, we find that student age is lower for treated schools at the 10% significance level only for the local linear specification. Taking into account that we are testing six student characteristics separately and using two specifications for each one, it comes as no surprise that we find one significant difference. The same reasoning holds for public schools. There, the only characteristic for which we find a significant difference between treated and control schools is father's income. However, the sign for the parametric specification is the opposite of the sign for the non-parametric specification.

[Insert Table 3 around here]

The finding that test score disclosure has no impact on the composition of students in schools is indicative that switching schools is not feasible in the short-run; not much time elapsed between the release of the average 2005 ENEM scores in 2006 and the 2007 ENEM. In this case, students (and their parents) could only react to test score disclosure by altering their effort.

Table 4 shows that test score disclosure had no consistently significant impact on school observable inputs in 2007. We consider the following inputs: the total number of enrolled students, the number of students enrolled in the third grade, the proportion of teachers with college degree, the ratios of computers, staff, and teachers to students, and the probability of having computer and science labs. The significant impact of test score disclosure on student enrollment and staff-to-student ratio in public schools is not robust to different specifications.

[Insert Table 4 around here]

In the same way that switching schools is likely to be infeasible for students in the short-run, changing school observable inputs is also likely to be infeasible for schools in the short-run. This can help explain why test score disclosure does not seem to affect school observable inputs.

5.2 Average Test Scores

Table 5 together with Figures 3 and 4 provide evidence that test score disclosure had a strong positive impact on average 2007 ENEM scores for private schools, but no impact on average 2007

ENEM scores for public schools. Figures 3 and 4 depict the linear relationship between average test scores and the number of graduating ENEM takers for private and public schools, respectively. The increase on average test scores for private schools above the treatment discontinuity is evident.

[Insert Figures 3 and 4 around here]

Table 5 reports parametric and non-parametric specifications of the relationship between test score disclosure and average 2007 ENEM scores.¹⁹ The result that for private schools, test score disclosure had a positive impact on average test scores is robust across all specifications we considered. We find that for private schools, test score disclosure increased average 2007 ENEM scores by 0.2 to 0.7 standard deviations of the private schools' test score distribution.²⁰ These are sizeable effects. On the other hand, we find that for public schools, test score disclosure had no statistically significant effect on average 2007 ENEM scores; test score disclosure increased average 2007 ENEM scores in public schools by -0.051 to 0.286 standard deviations of the public schools' test score distribution.

[Insert Table 5 around here]

5.3 Heterogenous Effects

It is reasonable to expect that the reaction of a school actor to test score disclosure depends on the average 2005 ENEM score in his school. In order to test for such heterogeneity, we split the sample of schools of a given type in two sub-samples, the schools with average 2005 ENEM scores above and below the median average score of the schools of the given type, and run the regression for the effect of test score disclosure on test scores for each of the two sub-samples separately. Note that when ranking schools according to their average 2005 ENEM scores, we included the schools that did not have their average ENEM scores released in 2005, so that the comparison is between schools that are similar ex-ante.

¹⁹We also ran non-parametric regressions using two different bandwidths, two different kernels (rectangular and triangular) and polynomial regressions of three different orders with two different windows for the running variable. The results are available upon request.

²⁰The results do not change if we condition on student and school characteristics.

Table 6 reports the impact of test score disclosure on 2007 ENEM scores for the two subsamples under consideration. For private schools, the impact of test score disclosure is positive for the schools below the median, but not significant for the schools above the median.²¹ For public schools, the impact of test score disclosure on test scores is negative for the schools above the median (local linear regressions), but not significant for the schools below the median. These results suggest that school actors perceive effort as a substitute for school quality.

[Insert Table 6 around here]

5.4 Confounding Factors and Robustness

We make use of a discontinuity in the disclosure rule for the average ENEM scores of schools to test for the impact of test score disclosure on a number of variables of interest. In order to test whether schools manipulated their number of ENEM takers in 2005, we check whether there is a jump in the frequency of schools at the treatment discontinuity. Figure 5 shows that there is no discernible jump at the treatment discontinuity. This evidence is not surprising. The ENEM is a voluntary exam and schools only learned about the test disclosure rule several months after the 2005 ENEM took place.

[Insert Figure 5 around here]

As further evidence that schools did not manipulate their number of ENEM takers in 2005, Figures 6 and 7 show that there is no discontinuity in the 2005 ENEM scores at the treatment discontinuity. Furthermore, we do not find statistically significant differences in student characteristics and school observable inputs in 2005 between treated and control schools.²²

²¹One could argue that the effect we find for the below-the-median treated private schools is due to a "catching up" effect. If this were the case, then one should also expect catching up to take place in control private schools, implying an insignificant impact of treatment on below-the-median private schools. It is possible that treatment may strengthen the catching up effect in private schools, though. This, however, would mean that test score disclosure does have an impact on student performance in private schools.

²²Tables with the regression results are available upon request. Another concern is that schools manipulated their number of ENEM takers in 2007. However, as already discussed in the text, the ENEM is a voluntary exam and the take-up rate is high. Besides, there is no reason to believe that treated and control schools could affect their students' decision to participate in the 2007 ENEM differently.

[Insert Figures 6 and 7 around here]

One could also conjecture that treated private schools with low average 2005 ENEM scores were more likely to close before 2007. If this were the case, then our results on the impact of test score disclosure on the average test scores of private schools would be biased due to selection among treated private schools. However, only 50 private schools in the entire sample close between 2005 and 2007. Moreover, there is no significant difference in school mortality between treated and control private schools. No public school closes between 2005 and 2007.

Finally, we falsify the treatment discontinuity and use cutoff points other than 10 (ENEM) takers for private schools. We run the non-parametric regression (local linear regressions with optimal bandwidth) for the impact of test score disclosure on test scores for all false cutoff points from 1 to 19 takers. Except for the false cutoff point of 12 takers, we find that the placebo treatment has no significant effect on test scores. Figure 8 depicts the z-test for the treatment effect for all false cutoff points tested.²³ The likely reason for why we find that test score disclosure has a negative impact on average test scores with the false cutoff point of 12 takers is the large increase in the average 2007 ENEM score for the private schools with 11 takers in 2005. One can then conjecture that this increase explains the effect of test score disclosure on test scores that we find for private schools. In order to test for this possibility, we run the true regression dropping from the sample the private schools with 9 and 11 takers in 2005. The effect remains. However, when we do the same with the false cutoff of 12 takers (now dropping the schools with 11 and 13 takers in 2005), the results become insignificant.²⁴

[Insert Figure 8 around here]

6 Test Score Disclosure and Market Incentives

We now develop a model of school and student behavior to help explain how test score disclosure can have a heterogeneous impact on test scores but, because of differences in market incentives

²³We do the same exercise for public schools and find no significant results for all false cutoff points tested for private schools. Results and graphs are available upon request.

²⁴Results are available upon request.

between public and private schools, increase average test scores only in private schools. The model we develop abstracts from the impact of test score disclosure on both the composition of students in schools and the school observable inputs. Doing so is reasonable given that we find no evidence that the observable characteristics of students or the school observable inputs changed from 2005 to 2007 in treated schools.

The rest of this section is organized as follows. We introduce the model in Subsection 6.1 and determine its unique equilibrium in Subsection 6.2. In Subsection 6.3, we use the model to study the impact of test score disclosure on test scores.

6.1 Setup

There is a finite number of schools, which are either public or private. For simplicity, we assume that each school has a representative (average) student. We do not distinguish between teachers and school managers and assume that each school has a single agent, which we refer to as a manager, responsible for the school's functioning. The only difference between public and private schools will be in terms of the incentives faced by their managers.

A student cares about his test (ENEM) score since it affects his future career. A manager in a private school also cares about the test score of the student in his school through a career concerns mechanism in which test scores signal school quality, and so affect school revenues.²⁵ Managers in public schools do not care about test scores.

Test Scores and School Quality The (expected) test score of a student in a given school is

$$\tau = \overline{\tau} - \frac{1}{2}(v_{\text{max}} - v + e_{\text{max}} - e + a_{\text{max}} - a)^2,$$

where $\overline{\tau}>0$ is a constant, $a\in[0,a_{\max}]$ is the student's effort, $e\in[0,e_{\max}]$ is the (school) manager's effort, and $v\in[0,v_{\max}]$ measures the school's quality.²⁶ A higher v means higher

²⁵The model we consider can be thought of as a reduced-form version of a dynamic model of managerial effort along the lines of Holmstrom [1999]. Considering a dynamic model of managerial effort would complicate the analysis without bringing any new insights.

 $^{^{26}}$ School managers can also engage in costly changes of school observable inputs such as hiring more qualified teachers. Since school quality and manager effort are substitutes, it does not matter for our analysis whether costly changes of school observable inputs represent changes in v or changes in e. Besides, we found no evidence that test

school quality in the sense that smaller effort, whether from the student or from the manager, is necessary for the same grade. The disutility of effort a for the student is c(a), while the disutility of effort e for the manager is $\lambda(e)$. The functions e and e are two times differentiable, strictly increasing, and strictly convex, with $\lambda'(0) = c'(0) = 0$. We also assume that c'(a) is convex in a.²⁷

A school's quality depends on both observable and unobservable characteristics of the school. The observable characteristics of a school are its observable inputs, while the unobservable characteristics of a school are the ability of its manager. Controlling for school observable inputs, the only differences in school quality are idiosyncratic differences in unobservable quality. Since we are interested in studying the impact of the disclosure of information about the unobservable component of school quality on the behavior of school actors, we omit the dependence of v on school observable inputs for ease of exposition. We assume that v is unknown to students and managers and that the value of v for each school is an independent random draw from a strictly positive probability density function ω .

Information Disclosure Besides being public or private, schools also differ in the information their students and managers have before making their effort choices. A school is treated if its manager and student observe a signal $\xi \in [\xi_{\min}, \xi_{\max}]$ about v before choosing their effort. The signal ξ captures the information about the ability of a school's manager that comes from observing the test score from a previous student of the school; a high ξ corresponds to a high test score. For each $v \in [0, v_{\max}]$, the signal $\xi \in [\xi_{\min}, \xi_{\max}]$ is drawn from a strictly positive probability density function $\ell(\cdot|v)$. We describe the event that a school is in the control group by saying that its manager and student observe the signal $\xi = \emptyset$.

We know from the empirical analysis that treated and control schools of each type do not differ in terms of their observable inputs and the characteristics of their students. This evidence validates the exogeneity of the treatment assignment. Hence, we assume that an independent random draw by nature determines whether a school is treated.

score disclosure has an impact on school observable inputs.

²⁷Note that a student's test score does not depend on her ability. Our analysis immediately extends to the case in which student ability affects test scores through $\bar{\tau}$. More generally, we can interpret the results of our model as describing the effect of test score disclosure on test scores controlling for student ability.

Let $\mu(\xi)$ be the posterior belief about v for a school with signal ξ . We assume the family $\{\ell(\cdot|v)\}_v$ of density functions is such that the likelihood ratio $\ell(\xi_1|v)/\ell(\xi_2|v)$ is strictly increasing in v for all $\xi_1 > \xi_2$ in $[\xi_{\min}, \xi_{\max}]$, that is, the family $\{\ell(\cdot|v)\}_v$ has the strict monotone likelihood ratio property (MLRP). In words, the greater the value added of a treated school, the more likely it is that its manager and student observe a high signal of school quality. Well-known results, see Milgrom [1981], show that if the family $\{\ell(\cdot|v)\}_v$ has the strict MLRP, then $\mu(\xi_1)$ dominates $\mu(\xi_2)$ in the strict first-order stochastic sense for all $\xi_1 > \xi_2$ in $[\xi_{\min}, \xi_{\max}]$.

Timing, Strategies, and Equilibrium The timing of events in a school is as follows. First, nature determines whether the school is treated or not. Then, the school's manager makes his choice of effort, followed by the student. This order of moves seems reasonable since it is much easier for a student to observe the effort of her school than the other way around. A strategy for a manager is a map $e: \{\emptyset\} \cup [\xi_{\min}, \xi_{\max}] \to [0, e_{\max}]$ such that $e(\xi)$ is the manager's effort if the signal he observes is ξ , while a strategy for a student is a map $a: [0, e_{\max}] \times (\{\emptyset\} \cup [\xi_{\min}, \xi_{\max}]) \to [0, a_{\max}]$ such that $e(\xi)$ is the student's effort if the manager's effort is $e(\xi)$ and the signal the student observes is ξ . An equilibrium for a school of a given type (public or private) is a strategy pair $e(\xi)$ such that: $e(\xi)$ is optimal for the manager given the school's type and the strategy a for the student; and $e(\xi)$ for all pairs $e(\xi)$, $e(\xi)$ is optimal for the student.

6.2 Equilibrium Behavior

Here, we compute the unique equilibrium of the game under consideration. We first determine the optimal choice of effort for a student given the signal ξ about the quality of her school and the effort e of her school's manager. Given the solution to the students' problem, we determine the optimal choice of effort for a manager as a function of the signal ξ about the quality of his school.

Student Effort Let $u(a, e, \xi)$ be the expected payoff to a student who chooses effort a when the manager in his school exerts effort e and the signal about school quality is ξ . Then

$$u(a, e, \xi) = \overline{\tau} - \frac{1}{2} \mathbb{E}_{\mu(\xi)} \left[(v_{\text{max}} - v + e_{\text{max}} - e + a_{\text{max}} - a)^2 \right] - c(a),$$

where $\mathbb{E}_{\mu(\xi)}$ denotes the expectation with respect to $\mu(\xi)$. Now let $\nu(\xi) = \mathbb{E}_{\mu(\xi)}[v]$ and denote the inverse of g(a) = c'(a) + a by h(x). Since g(a) is strictly increasing and convex in a, h(x) is strictly increasing and concave in x. Besides, $h'(x) = [1 + c''(h(x))]^{-1} < 1$, and so h(x) < x for all $x \in [0, g(a_{\max})]$ given that h(0) = 0. When $v_{\max} - \nu(\xi) + e_{\max} - e < c'(a_{\max})$, the choice $a^*(e, \xi)$ of student effort that maximizes $u(a, e, \xi)$ is

$$a^*(e,\xi) = h(v_{\text{max}} - \nu(\xi) + e_{\text{max}} - e + a_{\text{max}})$$
(2)

We assume that $v_{\text{max}} + e_{\text{max}} < c'(a_{\text{max}})$, so that (2) holds regardless of e and ξ .

Let \mathbb{E}_{ξ} denote the unconditional expectation with respect to ξ for treated schools. We show in Lemma 6 in the Appendix that $\mathbb{E}_{\xi}[\nu] = \nu(\emptyset)$, and that $\nu(\xi)$ is strictly increasing in ξ when $\xi \in [\xi_{\min}, \xi_{\max}]$, with $\nu(\xi_{\min}) < \nu(\emptyset) < \nu(\xi_{\max})$. Lemma 1 below follows immediately from the properties of h(x) and $\nu(\xi)$.

Lemma 1. $a^*(e,\xi)$ is strictly decreasing in both e and ξ . Moreover, $\partial a^*(e,\xi)/\partial e > -1$ and $\partial a^*(e,\xi)/\partial \xi > -\nu'(\xi)$.

The intuition for Lemma 1 is simple. By assumption, school quality, manager effort, and student effort are substitutes. Moreover, the production function for test scores is strictly concave in school quality and in student and manager effort. Hence, the (expected) marginal benefit of student effort is strictly decreasing in manager effort and expected school quality. However, the marginal cost of effort for a student is strictly increasing in the student's effort, and so the rate at which a student decreases her effort in response to an increase in either manager effort or expected school quality is smaller than the rate at which manager effort and expected school quality increase.

Manager Effort It is clear that the optimal choice of effort for managers in public schools is zero regardless of the signal they observe. Consider now the behavior of managers in private schools. Let $\pi(e, \xi)$ be the expected payoff to a manager who exerts effort e when the signal about school quality is ξ and the effort choice of the student in the manager's school is given by (2). Then

$$\pi(e,\xi) = \overline{\tau} - \frac{1}{2} \mathbb{E}_{\mu(\xi)} \left[(v_{\max} - v + e_{\max} - e + a_{\max} - a^*(e,\xi))^2 \right] - \lambda(e).$$

Note that we implicitly assume that if a school is treated, then the treatment affects the school manager's payoff only through ξ . However, if the impact on a school of its student's test score depends on whether this score becomes public or not, then managers in treated schools would face different incentives than managers in control schools if managers believe the probability a school is treated depends on whether the school was treated before. For reasons that were discussed in Section 5, this is not the case in our environment, though, and so the assumption that treatment affects a manager's payoff only through ξ is justified.

Let
$$\eta(x)=x-h(x)$$
 and $H(x)=\eta(x)\eta'(x)$. Then
$$\frac{\partial\pi}{\partial e}(e,\xi)=H(v_{\max}-\nu(\xi)+e_{\max}-e+a_{\max})-\lambda'(e).$$

Since H(x) is strictly increasing in x, $\partial \pi(e,\xi)/\partial e$ is strictly decreasing in e. So, there is a unique choice of manager effort $e^*(\xi)$ that maximizes $\pi(e,\xi)$. Note that $e^*(\xi)$ is interior if $v_{\rm max} - \nu(\xi) + a_{\rm max} < \lambda'(e_{\rm max})$, in which case $e^*(\xi)$ is defined implicitly by

$$\lambda'(e) = H(v_{\text{max}} - \nu(\xi) + e_{\text{max}} - e + a_{\text{max}}).$$
 (3)

We assume that $v_{\rm max} + a_{\rm max} < \lambda'(e_{\rm max})$, so that $e^*(\xi)$ is defined by (3) regardless of the signal ξ .²⁸ It is easy to see that H(x) is linear in x if c(a) is quadratic in a. We show in Lemma 7 in the Appendix that H(x) is convex in x if c''(a) is convex in a and c'(a)/c''(a) is nondecreasing in a. The assumption that c''(a)/c'(a) is nonincreasing is very mild; it holds as long as the growth rate of c'(a) is exponential or subexponential. In what follows, we assume that the cost function c satisfies the assumptions of Lemma 7.

Now observe that since H(x) is strictly increasing in x and $\nu(\xi)$ is strictly increasing in ξ when $\xi \in [\xi_{\min}, \xi_{\max}]$, the marginal benefit of effort for a manager in a treated school is strictly decreasing in ξ . The next result follows immediately.

Lemma 2. $e^*(\xi)$ is strictly decreasing in ξ for treated private schools.

The intuition for why $\partial \pi(e,\xi)/\partial \xi$ is strictly decreasing in ξ for treated schools is as follows. An increase in ξ has two opposing effects. On the one hand, a higher expected school quality

The assumptions that $v_{\text{max}} + a_{\text{max}} < \lambda'(e_{\text{max}})$ and $v_{\text{max}} + e_{\text{max}} < c'(a_{\text{max}})$ are mutually compatible.

decreases the marginal benefit of manager effort. On the other hand, by Lemma 1, an increase in ξ reduces student effort, which increases the marginal benefit of manager effort. However, also by Lemma 1, the rate at which student effort decreases with an increase in ξ is smaller than the rate at which expected school quality increases with an increase in ξ . Thus, the first, negative, effect of an increase in ξ on the marginal benefit of manager effort dominates and $e^*(\xi)$ is strictly decreasing in ξ for treated private schools.

Since $\nu(\xi_{\min}) < \nu(\emptyset) < \nu(\xi_{\max})$, managers in treated private schools can exert more or less effort than managers in control private schools depending on the signal ξ they observe. Thus, it is not clear how the average effort of managers in treated private schools compares with the effort of managers in control private schools. Lemma 3 below provides conditions under which the average effort of managers in treated private schools is greater than the effort of managers in control private schools. This result is important when we study the impact of test score disclosure on average test scores. Let $G_1(y)$ and $G_2(y)$ be two functions, with $G_1(y)$ strictly increasing and $G_2(y)$ convex. We say that $G_1(y)$ is less convex than $G_2(y)$ if $G_1^{-1}(G_2(y))$ is strictly convex. The proof of Lemma 3 is in the Appendix.

Lemma 3. Suppose $\lambda'(e)$ is less convex than H(x). Then $\mathbb{E}_{\xi}[e^*] > e^*(\emptyset)$.

Note that regardless of the function H(x), the assumption of Lemma 3 is satisfied if $\lambda'(e)$ is strictly concave in e. Also note that if c(a) is quadratic in a, then the assumption of Lemma 3 only holds if $\lambda'(e)$ is strictly concave in e. It follows immediately from the proof of Lemma 7 in the Appendix that H(x) is strictly convex in x if c'(a) is strictly convex in a. In this case, the assumption of Lemma 3 can be satisfied when $\lambda'(e)$ is strictly convex.

The Equilibrium Putting together the optimal behavior of students and managers derived above, we obtain the equilibria for public and private schools. Let (e^0, a^0) be the strategy pair given by $e^0 \equiv 0$ and $a^0(e, \xi) = a^*(e, \xi)$. By construction, (e^0, a^0) is the unique equilibrium for public schools. Now let (e^1, a^1) be such that $e^1(\xi)$ is given by (3) and $a^1 = a^0$. By construction, (e^1, a^1) is the unique equilibrium for private schools. In what follows, for ease of exposition, we sometimes refer to public schools as schools of type 0 and to private schools as schools of type 1, and use superscripts to denote a school's type.

6.3 The Impact of Test Score Disclosure

We now study the impact of test score disclosure on test scores. We first consider the heterogeneous effect of test score disclosure on test scores. Then we consider the impact of test score disclosure on average test scores. In what follows, let $\kappa = v_{\rm max} + e_{\rm max} + a_{\rm max}$

Heterogeneous Effects The total effort in a control school of type s is $T_0^s = \mathsf{e}^s(\emptyset) + a^*(\mathsf{e}^s(\emptyset), \emptyset)$, while the total effort in a treated school of type s with signal ξ about school quality is $T_1^s(\xi) = \mathsf{e}^s(\xi) + a^*(\mathsf{e}^s(\xi), \xi)$. Notice that $T_1^0(\xi) = a^*(0, \xi)$ is strictly decreasing in ξ by Lemma 1. Now observe from Lemmas 1 and 2 that

$$\frac{dT_1^1}{d\xi}(\xi) = \frac{de^*}{d\xi}(\xi) \left[1 + \frac{\partial a^*}{\partial e}(e^*(\xi), \xi) \right] + \frac{\partial a^*}{\partial \xi}(e^*(\xi), \xi) < 0,$$

and so $T_1^1(\xi)$ is also strictly decreasing in ξ . In words, we know that a student exerts more effort if the manager from her school exerts less effort. However, we also know that when a manager decreases his effort, the resulting increase in effort by the student in the manager's school is less than the reduction in the manager's effort. Thus, $T_1^1(\xi)$ is strictly decreasing in ξ since both $e^*(\xi)$ and $a^*(e,\xi)$ are strictly decreasing in ξ . Also notice that $T_1^s(\xi_{\min}) > T_0^s > T_1^s(\xi_{\max})$ for each $s \in \{0,1\}$ given that $\nu(\xi_{\min}) < \nu(\emptyset) < \nu(\xi_{\max})$. The following result summarizes.

Lemma 4.
$$T_1^s(\xi)$$
 is strictly decreasing in ξ with $T_1^s(\xi_{\min}) > T_0^s > T_1^s(\xi_{\max})$ for $s = 0, 1$.

Lemma 4 shows that test score disclosure has a heterogeneous impact on the effort of students and managers, and thus has a heterogeneous impact on test scores. In order to relate Lemma 4 to our empirical results, let $\Omega(\cdot)$ be the cumulative density function of the unconditional distribution of the signal ξ of school quality. In our model, the signal ξ about school quality corresponds to the average 2005 ENEM score. Hence, if $\xi_{(1;n)}$ is such that $\Omega(\xi_{(1;n)}) = 1 - 1/n$, then

$$A_1^s(1;n) = \overline{\tau} - \frac{1}{2} \int_{\xi_{(1;n)}}^{\xi_{\text{max}}} \mathbb{E}_{\mu(\xi)} \left[(\kappa - v - T_1^s(\xi))^2 \right] d\Omega(\xi)$$

and

$$A_0^s(1;n) = \overline{\tau} - \frac{1}{2} \int_{\xi_{(1;n)}}^{\xi_{\text{max}}} \mathbb{E}_{\mu(\xi)} \left[(\kappa - v - T_0^s)^2 \right] d\Omega(\xi)$$

are, respectively, the average test scores of the treated and control schools with a signal ξ of school quality in the highest n-quantile. Since $\lim_{n\to\infty}\xi_{(1;n)}=\xi_{\max}$, Lemma 4 implies that $A_1^s(1;n)<$ $A_0^s(1;n)$ if n is large enough. Similarly, if $A_1^s(n-1;n)$ and $A_0^s(n-1;n)$ are, respectively, the average test scores of the treated and control schools with a signal ξ of school quality in the lowest n-quantile, then Lemma 4 implies that $A_1^s(n-1;n) > A_0^s(n-1;n)$ if n is large enough.²⁹ We have then established the following result.

Proposition 1. $\overline{A}_1^s(n) < \overline{A}_0^s(n)$ and $\underline{A}_1^s(n) > \underline{A}_0^s(n)$ if n is large enough.

Proposition 1 shows that our model can explain our empirical findings concerning the heterogeneous effect of test score disclosure on student performance.³⁰

Average Test Scores The average test score A_0^s in a control school of type s and the average test score A_1^s in a treated school of type s are

$$A_0^s = \overline{\tau} - \frac{1}{2} \mathbb{E}_{\mu(\emptyset)} \left[(\kappa - v - T_0^s)^2 \right]$$

and

$$A_1^s = \overline{\tau} - \frac{1}{2} \mathbb{E}_{\xi} \left\{ \mathbb{E}_{\mu(\xi)} \left[(\kappa - v - T_1^s(\xi))^2 \right] \right\}.$$

Since managers in public schools never exert effort, only the students in public schools react to test score disclosure. The assumption that c''(a)/c'(a) is nonincreasing in a implies that the average test score in a treated public school is never smaller than the average test score in a control public school; see the Appendix for a proof.

Lemma 5. $A_1^0 \ge A_0^0$.

In private schools, both managers and students react to test score disclosure. Given that h(x)is strictly concave in x, Jensen's inequality implies that if the average effort of managers in treated private schools is greater than the effort of managers in control private schools, then the average

²⁹The average $A_k^s(n-1;n)$ is obtained from the average $A_k^s(1;n)$ by changing the integration limits from $\xi_{(1;n)}$ to ξ_{\max} to ξ_{\min} to $\xi_{(n-1;n)}$, where $\xi_{(n-1;n)}$ is such that $\Omega(\xi_{(n-1;n)}) = 1/n$.

30 Table 6 only reports the heterogenous effect of test score disclosure for the case of n=2. We obtain similar

results for higher quantiles. These results are available upon request.

effort of students in treated private schools is smaller than the effort of students in control private schools. This makes intuitive sense since the effort of students and managers are substitutes. Thus, it is not clear a priori whether test score disclosure can increase average test scores in private schools, let alone increase average test scores in private schools by more than it increases in public schools. The last result in this section provides conditions under which test score disclosure leads to a greater increase in average test scores in private schools than in public schools. Note that $\lambda'(e)e$ is convex if $\lambda'(e)$ is convex. More generally, $\lambda'(e)e$ is convex as long as $\lambda'(e)$ is not "too" concave. The proof of Proposition 2 is in the Appendix.

Proposition 2. If $\lambda'(e)e$ is convex and $\lambda'(e)$ is less convex than H(x), then $A_1^1 - A_0^1 > A_1^0 - A_0^0 \geq 0$.

Proposition 2 shows that if managers in private schools face stronger incentives for performance than managers in public schools, then test score disclosure can increase average test scores in private schools by more than it increases average test scores in public schools. Besides, an immediate consequence of the proof of Lemma 5 is that if c(a) is quadratic, then test score disclosure has no effect on average test scores in public schools. More generally, as long as c(a) does not differ too much from a quadratic function, test score disclosure has a small impact on average test scores in public schools. Thus, our model shows how differences in incentives for performance between public and private schools can help explain our empirical findings concerning the effect of test score disclosure on average test scores.

7 Conclusion

This paper uses a discontinuity on the rule for the disclosure of the average ENEM score of schools in Brazil to identify the informational effect of test score disclosure on student performance, student composition, and school observable inputs in public and private schools in the São Paulo Metropolitan area. We find that test score disclosure has no effect on student composition and school observable inputs in both public and private schools. We also find that test score disclosure has a heterogeneous effect on student performance in both public and private schools, but only increases average test scores in private schools.

Our empirical findings suggest that test score disclosure affects student performance by changing the effort of students (and their parents), teachers, and school managers. Since in Brazil, teachers and managers in public schools face weaker market incentives than teachers and managers in private schools, our results provide evidence that test score disclosure has an impact on the market incentives faced by private schools. We develop a model of school and student behavior to show how differences in incentives faced by teachers and managers in different types of school can help explain how test score disclosure can have a heterogeneous impact on test scores in both public and private schools, but only increase average test scores in private schools.

8 Appendix

Lemma 6 and Proof

Lemma 6. $\mathbb{E}_{\xi}[\nu] = \nu(\emptyset)$. Moreover, $\nu(\xi)$ is strictly increasing in ξ when $\xi \in [\xi_{\min}, \xi_{\max}]$, with $\nu(\xi_{\min}) < \nu(\emptyset) < \nu(\xi_{\max})$.

Proof. The fact that $\nu(\xi)$ is strictly increasing in ξ follows immediately from the fact that if $\xi_1, \xi_2 \in [\xi_{\min}, \xi_{\max}]$ are such that $\xi_1 > \xi_2$, then $\mu(\xi_1)$ dominates $\mu(\xi_2)$ in the strict first-order stochastic sense. The fact that $\mathbb{E}_{\xi}[\nu] = \nu(\emptyset)$ follows easily from Bayes' rule. To finish, note that if $\nu(\xi_{\min}) \geq \nu(\emptyset)$, then $\nu(\xi)$ strictly increasing in ξ implies that $\mathbb{E}_{\xi}[\nu] > \nu(\emptyset)$, a contradiction. Thus, $\nu(\xi_{\min}) < \nu(\emptyset)$. The same argument shows that $\nu(\xi_{\max}) > \nu(\emptyset)$.

Proof of Lemma 3

Let $F = (\lambda')^{-1} \circ H$, $X(\xi) = -F'(v_{\text{max}} - \nu(\emptyset) + e_{\text{max}} - e^*(\xi) + a_{\text{max}})$, and $Y(\xi) = \nu(\xi) - \nu(\emptyset)$. Now note that

$$\mathbb{E}_{\xi}[e^*] = \mathbb{E}_{\xi} \left[F(v_{\text{max}} - \nu + e_{\text{max}} - e^* + a_{\text{max}}) \right]$$

$$> \mathbb{E}_{\xi} \left[F(v_{\text{max}} - \nu(\emptyset) + e_{\text{max}} - e^* + a_{\text{max}}) \right] + \mathbb{E}_{\xi} \left[XY \right]$$

$$\geq F(v_{\text{max}} - \nu(\emptyset) + e_{\text{max}} - \mathbb{E}_{\xi}[e^*] + a_{\text{max}}) + \mathbb{E}_{\xi} \left[XY \right],$$

where the equality follows from (3), the first inequality follows from the strict convexity of F, and the second inequality follows from Jensen's inequality. Since $X(\xi)$ and $Y(\xi)$ are nondecreasing in ξ , Theorem 22 in Milgrom and Weber [1982] implies that $\mathbb{E}_{\xi}[XY] \geq \mathbb{E}_{\xi}[X]\mathbb{E}_{\xi}[Y]$. Moreover, $\mathbb{E}_{\xi}[\nu] = \nu(\emptyset)$ by Lemma 6. Therefore,

$$\mathbb{E}_{\xi}[e^*] > F(v_{\max} - \nu(\emptyset) + e_{\max} - \mathbb{E}_{\xi}[e^*] + a_{\max}).$$

The desired result follows from (3).

Lemma 7 and Proof

Lemma 7. H is convex if c''(a) is convex in a and c''(a)/c'(a) is nonincreasing in a.

Proof. Note that g(h(x)) = x implies that $\eta(x) = c'(h(x))$. Hence, H(x) = c'(h(x))[1 - h'(x)]. Given that $h'(x) = [1 + c''(h(x))]^{-1}$, straightforward algebra shows that $H'(x) = \Lambda(h(x))$, where

$$\Lambda(h) = \frac{c''(h)^2}{[1 + c''(h)]^2} + \frac{c'''(h)c'(h)}{[1 + c''(h)]^3},$$

Now note that

$$\Lambda'(h) = \frac{3c'''(h)c''(h) + c^{(iv)}(h)c'(h)}{[1 + c''(h)]^3} - \frac{3c'''(h)c'(h)}{[1 + c''(h)]^4}$$

Then $\Lambda'(h) \geq 0$, since c''(a) is convex and c'(a)/c''(a) nondecreasing in a implies that $c'''(a)c'(a) \leq (c''(a))^2$. The desired results follows from the fact that h(x) is strictly increasing in x.

Proof of Lemma 5

It follows from Bayes' rule that $\mathbb{E}_{\mu(\emptyset)}[f] = \mathbb{E}_{\xi} \left\{ \mathbb{E}_{\mu(\xi)}[f] \right\}$ for any (measurable) function f. Hence, $\mathbb{E}_{\mu(\emptyset)}[(\kappa - v)^2] = \mathbb{E}_{\xi} \left\{ \mathbb{E}_{\mu(\xi)}[(\kappa - v)^2] \right\}$, and so

$$A_1^0 - A_0^0 \propto -2(\kappa - \nu(\emptyset))h(\kappa - \nu(\emptyset)) + h(\kappa - \nu(\emptyset))^2 + \mathbb{E}_{\xi}[2(\kappa - \nu)h(\kappa - \nu) - h(\kappa - \nu)^2]$$
$$= \mathbb{E}_{\xi}[M(\kappa - \nu)] - M(\kappa - \nu(\emptyset)),$$

where $M(x) = x^2 - \eta(x)^2$. Since $\mathbb{E}_{\xi}[\nu] = \nu(\emptyset)$, Jensen's inequality implies that $A_1^0 \geq A_0^0$ when M(x) is convex. Now observe that M(x) is convex if, and only if, $H'(x) \leq 1$. It follows

immediately from the proof of Lemma 7 that $H'(x) \leq 1$ if, and only if,

$$c''(h(x))^{2} + c''(h(x))^{3} + c'''(h(x))c'(h(x)) \le [1 + c''(h(x))]^{3},$$

which is satisfied since h(x) is strictly increasing in x and $c'''(a)c'(a) \leq (c''(a))^2$ by assumption.

Proof of Proposition 2

For each $z \in [0,1]$ and $\xi \in [\xi_{\min}, \xi_{\max}]$, let

$$\Gamma_0^z = \frac{1}{2} \mathbb{E}_{\mu(\emptyset)} \left[\left(\kappa - v - z \mathbf{e}^1(\emptyset) - h(\kappa - \nu(\emptyset) - z \mathbf{e}^1(\emptyset)) \right)^2 \right]$$

and

$$\Gamma_1^z(\xi) = \frac{1}{2} \mathbb{E}_{\mu(\xi)} \left[\left(\kappa - v - z \mathbf{e}^1(\xi) - h(\kappa - \nu(\xi) - z \mathbf{e}^1(\xi)) \right)^2 \right].$$

Now let $\Delta(z)$, with $z \in [0,1]$, be such that $\Delta(z) = \Gamma_0^z - \mathbb{E}_{\xi}[\Gamma_1^z]$. By construction, $\Delta(1) = A_1^1 - A_0^1$ and $\Delta(0) = A_1^0 - A_0^0$. Straightforward algebra shows that

$$\begin{split} \Delta'(z) &= -H(\kappa - \nu(\emptyset) - z \mathrm{e}^1(\emptyset)) \mathrm{e}^1(\emptyset) + \mathbb{E}_{\xi} \left[H(\kappa - \nu - z \mathrm{e}^1) \mathrm{e}^1 \right] \\ &= \mathbb{E}_{\xi} [\lambda'(z \mathrm{e}^1) \mathrm{e}^1] - \lambda'(z \mathrm{e}^1(\emptyset)) \mathrm{e}^1(\emptyset) \\ &\geq \lambda' \left(z \mathbb{E}_{\xi} [\mathrm{e}^1] \right) \mathbb{E}_{\xi} [\mathrm{e}^1] - \lambda'(z \mathrm{e}^1(\emptyset)) \mathrm{e}^1(\emptyset), \end{split}$$

where the second equality follows from (3) and the inequality follows from Jensen's inequality. Hence, $\Delta'(z) > 0$ for all $z \in (0,1]$, so that $\Delta(1) > \Delta(0)$.

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Tables and Figures

Table 1: Descriptive Statistics - Private Schools

	Less th	an 10 exa	m takers	10 to	10 to 19 exam takers			More than 19 takers		
	N	Mean	S.D.	N	Mean	S.D.	N	Mean	S.D.	
Standardized Test Score	2,310	-0.55	0.99	5,125	-0.37	0.99	44,371	0.07	0.98	
Male	1,879	0.45	0.5	4,256	0.43	0.5	35,873	0.44	0.5	
Age	1,874	17.39	0.81	4,241	17.39	0.9	35,799	17.37	0.83	
White	1,864	0.76	0.43	4,231	0.78	0.42	35,672	0.79	0.41	
Father w/ College Degree	1,790	0.36	0.48	4,091	0.42	0.49	34,822	0.54	0.5	
Mother w/ College Degree	1,827	0.38	0.49	4,178	0.42	0.49	35,322	0.52	0.5	
Income ≤ 10×Minimum Wage	1,846	0.7	0.46	4,159	0.64	0.48	35,125	0.49	0.5	
# of Students who Work	411	0.67	0.47	834	0.67	0.47	5,883	0.69	0.46	
# of Students Enrolled in Extra Classes	1,846	0.16	0.37	4,211	0.17	0.38	35,529	0.22	0.41	
# of Students at High School	2,304	62.04	36.44	5,101	89.57	52.32	44,060	447.62	414.96	
# of Teachers	2,304	25.45	16.82	5,101	27.2	19.47	44,060	93.23	133.89	
% of Teachers w/ College Degree	2,304	1.01	0.36	5,101	1.02	0.38	44,060	0.92	0.42	
# of Computers	2,282	20.03	32.73	5,091	29.18	35.54	44,056	91	108.64	
Teacher-to-Student ratio	2,304	0.47	0.34	5,101	0.35	0.37	44,060	0.25	0.24	
Computer Lab	2,310	0.71	0.45	5,125	0.81	0.4	44,371	0.81	0.4	
Science Lab	2,310	0.23	0.42	5,125	0.28	0.45	44,371	0.21	0.4	
Library	2,310	0.51	0.5	5,125	0.48	0.5	44,371	0.38	0.49	
Internet Access	2,304	0.99	0.06	5,124	1	0	44,265	0.99	0.02	
% of ENEM Takers	2,289	0.61	0.22	5,070	0.69	0.18	44,056	0.81	0.18	

Sources: ENEM microdata and School Census

Table 2: Descriptive Statistics - Public Schools

	Less	than 10 ex	am takers	10 to	19 exam	takers	More than 19 takers		
	N	Mean	S.D.	N	Mean	S.D.	N	Mean	S.D.
Standardized Test Scores	420	-0.31	0.87	2,970	-0.34	0.82	221,448	0.01	1
Male	344	0.35	0.48	2,493	0.38	0.49	185,527	0.38	0.49
Age	342	19.22	2.64	2,487	18.89	2.48	184,848	18.4	2.15
White	341	0.39	0.49	2,475	0.4	0.49	184,247	0.5	0.5
Father w/ College Degree	300	0.03	0.16	2,224	0.02	0.13	168,159	0.06	0.23
Mother w/ College Degree	331	0.03	0.16	2,401	0.02	0.14	179,760	0.06	0.23
Income ≤ 10×Minimum Wage	332	0.99	0.09	2,405	0.99	0.08	181,551	0.98	0.16
# of Students who Work	179	0.65	0.48	1403	0.67	0.47	94,525	0.7	0.46
# of Students enrolled in Extra Classes	333	0.06	0.24	2,426	0.05	0.22	181,305	0.09	0.28
# of Students at High School	400	173.69	91.61	2,923	257.41	155.01	216,956	793.01	455.26
# of Teachers	400	39.18	25.21	2,923	51.34	42.71	216,956	110.11	111.3
% of Teachers w/ College Degree	400	1.09	0.48	2,923	1.16	0.7	216,956	0.96	0.44
# of Computers	302	5.66	4.51	2,773	8.21	4.74	215,156	14.42	27.44
Teacher-to-Student ratio	400	0.23	0.11	2,923	0.21	0.12	216,956	0.15	0.11
Computer Lab	420	0.65	0.48	2,970	0.83	0.38	221,448	0.95	0.23
Science Lab	420	0.27	0.45	2,970	0.42	0.49	221,448	0.38	0.49
Library	420	0.8	0.4	2,970	0.87	0.34	221,448	0.97	0.18
Internet Access	389	0.97	0.17	2,940	0.91	0.28	220,771	0.98	0.13
% of ENEM Takers	364	0.41	0.24	2,655	0.43	0.24	215,756	0.57	0.23

Sources: ENEM microdata and School Census

Table 3: Effects on 2007 Student Composition

14010	Table 3. Effects on 2007 Student Composition										
		Private			Public						
Specification	Coefficient	Stand. Error	# of obs.	Coefficient	Stand. Error	# of obs.					
Male											
Local Linear	-0.028	0.060	3,104	-0.034	0.106	1,538					
Quadratic	0.009	0.068	3,104	0.003	0.098	1,538					
Age											
Local Linear	-0.170*	0.096	3,091	0.732	0.797	1,532					
Quadratic	-0.211	0.135	3,091	2.405**	0.952	1,532					
White											
Local Linear	0.013	0.049	3,078	-0.011	0.080	1,521					
Quadratic	0.020	0.060	3,078	-0.031	0.092	1,521					
Father w/ College Degree											
Local Linear	0.055	0.073	2,973	-0.018	0.033	1,363					
Quadratic	0.084	0.088	2,973	-0.054*	0.030	1,363					
Mother w/ College Degree											
Local Linear	0.073	0.063	3,037	-0.041	0.032	1,479					
Quadratic	0.111	0.078	3,037	-0.046	0.028	1,479					
Income ≤ 10×Minimum Wage											
Local Linear	-0.107	0.105	3,041	-0.009*	0.005	1,489					
Quadratic	-0.150	0.106	3,041	0.025**	0.012	1,489					

Note: *p < 0.1, **p < 0.05. Treatment: schools with 10 or more ENEM takers in 2005. Sample of schools with 1 to 19 takers in 2005

Source: ENEM microdata

Table 4: Effects on 2007 School Inputs

		Private			Public	
Specification	Coefficient	Stand. Error	# of obs.	Coefficient	Stand. Error	# of obs.
Number of Students						
Local Linear	25.823	16.524	3,261	114.387**	55.773	1,670
Quadratic	18.184	20.992	3,273	68.037	102.069	1,670
Number of Students in 3^{rd} Grade						
Local Linear	4.189	3.851	3,261	18.796	21.906	1,638
Quadratic	3.380	7.649	3,261	-5.621	18.794	1,638
Proportion of Teachers w/ College Degree						
Local Linear	-0.000	0.032	3,273	0.003	0.006	1,670
Quadratic	0.012	0.022	3,273	0.003*	0.013	1,670
Computer-to-Student Ratio						
Local Linear	0.181	0.157	3,218	-0.035	0.035	1,464
Quadratic	0.198	0.169	3,218	-0.040	0.030	1,464
Staff-to-Student Ratio						
Local Linear	0.008	0.141	3,273	-	_	1,670
Quadratic	0.043	0.280	3,273	0.266**	0.126	1,670
Teacher-to-Student Ratio						
Local Linear	-0.064	0.078	3,273	0.021	0.039	1,670
Quadratic	-0.004	0.094	3,273	0.045	0.039	1,670
Computer Lab						
Local Linear	0.079	0.237	3,302	-0.166	0.127	1,737
Quadratic	0.013	0.229	3,302	-0.241	0.177	1,737
Science Lab						
Local Linear	0.042	0.169	3,302	-0.031	0.029	1,737
Quadratic	0.124	0.206	3,302	0.014	0.058	1,737

Note: *p < 0.1, **p < 0.05.

Treatment: schools with 10 or more ENEM takers in 2005. Sample of schools with 1 to 19 takers in 2005

Source: School Census

Table 5: Effects on 2007 Average Test Score

		Private			Public	
Specification	Coefficient	Stand. Error	# of obs.	Coefficient	Stand. Error	# of obs.
Local Linear (Opt. BW)	0.536**	0.271	3,302	0.162	0.240	1,737
Local Linear ($2 \times Opt. BW$)	0.371**	0.169	3,302	0.086	0.163	1,737
10-Takers Window						
Mean Differences	0.166**	0.070	3,302	-0.042	0.066	1,737
Linear	0.161	0.136	3,302	0.139	0.131	1,737
Quadratic	0.518**	0.219	3,302	-0.051	0.255	1,737
5-Takers Window						
Mean Differences	0.130	0.084	2,080	0.019	0.067	836
Linear	0.380**	0.175	2,080	0.117	0.217	836
Quadratic	0.749**	0.339	2,080	0.286	0.309	836

Note: *p < 0.1, **p < 0.05.

Treatment: schools with 10 or more ENEM takers in 2005.

10-Takers Window: Sample of schools with 1 to 19 takers in 2005

5-Takers Window: Sample of schools with 5 to 14 takers in 2005

Table 6: Heterogenous Effects on 2007 Scores (by 2005 Scores)

		Below Median		Above Median			
Specification	Coefficient	Stand. Error	# of obs.	Coefficient	Stand. Error	# of obs.	
Private							
Local Linear (Opt. BW)	0.469*	0.281	2,365	0.168	0.929	667	
Local Linear (2 × Opt. BW)	0.351**	0.169	2,365	0.045	0.434	667	
Quadratic	0.488**	0.229	2,365	-0.130	0.545	667	
Public							
Local Linear (Opt. BW)	0.171	0.239	1,165	-0.256**	0.013	572	
Local Linear (2 \times Opt. BW)	0.105	0.185	1,165	-0.358**	0.042	572	
Quadratic	-0.042	0.264	1,165	-0.039	0.366	572	

Note: *p < 0.1, **p < 0.05.

Treatment: schools with 10 or more ENEM takers in 2005.

Sample of schools with 1 to 19 takers in 2005

Notas Médias do Enem dos alunos concluintes do Ensino Médio por escola.											
Modalidade: Ensino I	Médio Regular		Munic	ipio: São Paulo		Rede de Ensin	Rede de Ensino: Privada				
UF: SP			Locali	zação: Urbana		Dep. Administr	Dep. Administrativa: Todas				
Buscar nos seus resultados											
Escola 🗲	Participantes Prova Objetiva ≅	Média em Linguagens, Códigos [©]	Média em Matemática ≠	Média em Ciéncias Humanas [©]	Média em Ciências da Natureza ^{ra}	Média nas Objetivas *	Participantes Redação ª	Média Redação €	Média Total (Redação + Objetivas)		
		ex e	1 2 3	4 5 6 7	8 9 10	0 30					
ACTIVE COLEGIO®	4	sc	sc	sc	sc	sc	4	sc	S		
ADVENTISTA CIDADE ADEMAR ESCOLA	9	sc	sc	sc	sc	sc	9	sc	s		
ADVENTISTA COLEGIO DE INTERLAGOS	18	561,62	595,90	563,26	582,40	575,79	18	538,89	557,3		
ADVENTISTA DA LIBERDADE COLEGIO	27	557,66	545,56	561,15	580,46	561,21	27	634,26	597,7		
ADVENTISTA DE CAMPO LIMPO COLEGIO Q	11	565,15	548,19	525,99	527,04	541,59	11	684,09	612,8		
ADVENTISTA DE TUCURUVI COLEGIO (1)	19	517,42	519,49	527,24	528,08	523,06	19	606,58	564,8		
ALIADO COLEGIO UNIDADE JARDIM JAPAO 🖳	4	sc	sc	sc	sc	sc	4	sc	S		

Figure 1: Screenshot from INEP's Website. Column 1 lists the school names, while Column 2 lists the number of ENEM takers in each school. The average school scores at the different subjects covered by ENEM are listed in Columns 3 to 6, while the average school score at the essay is listed in Column 9. Column 10 lists the average ENEM score for each school. Only schools with 10 or more ENEM takers have their ENEM scores released.

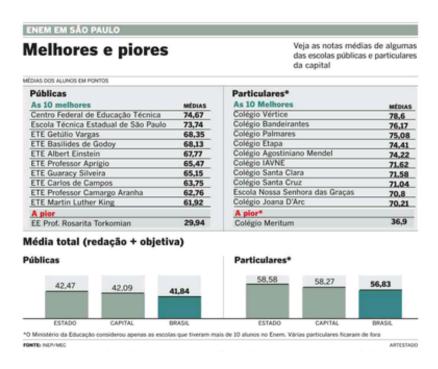


Figure 2: Newspaper ranking from O Estado de São Paulo, one of the four major newspapers in Brazil, published on February 9th of 2006 showing average 2005 ENEM scores for schools in the city of São Paulo. The column on the left shows the 10 public schools with the highest average score, as well as the public school with the lowest average score. The column on the right does the same for private schools.

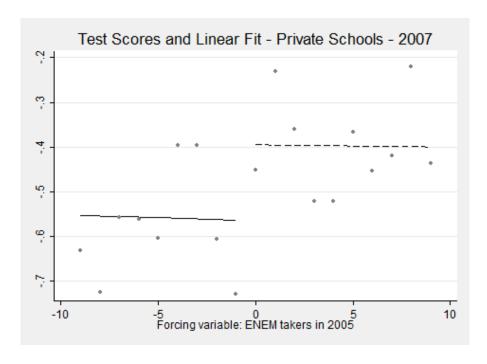


Figure 3: 2007 ENEM Performance for Private Schools

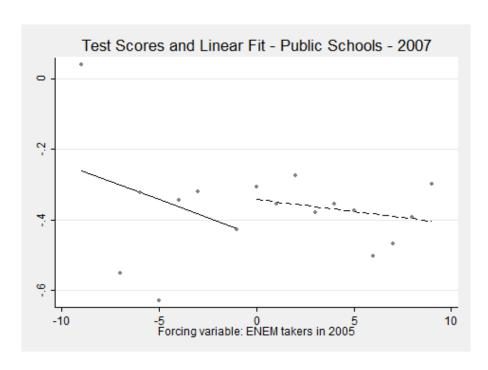


Figure 4: 2007 ENEM Performance for Public Schools

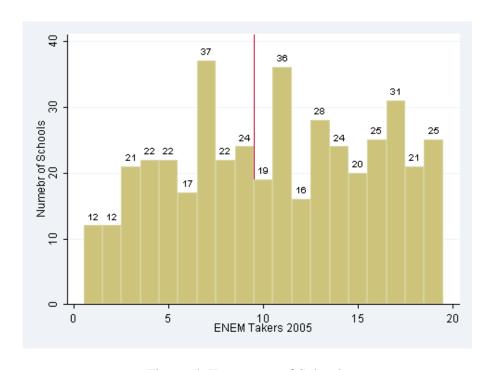


Figure 5: Frequency of Schools

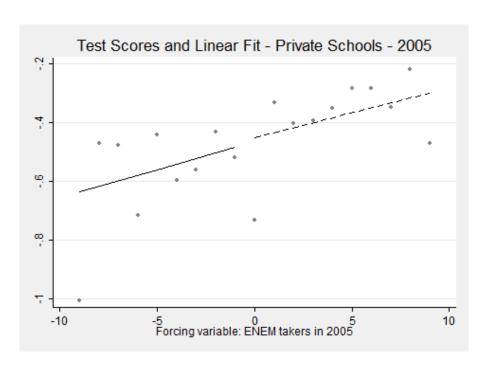


Figure 6: 2005 ENEM Performance for Private Schools

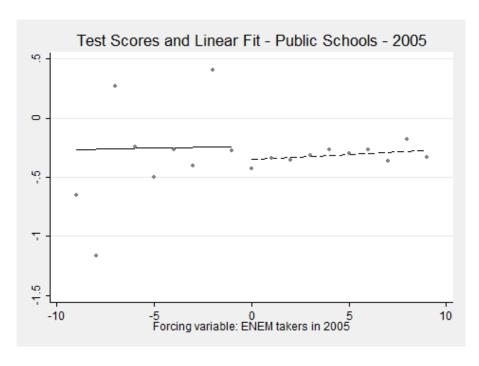


Figure 7: 2005 ENEM Performance for Public Schools

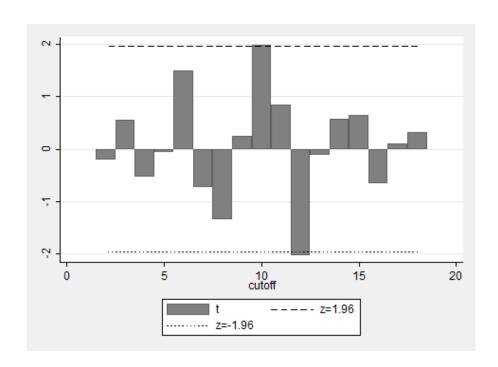


Figure 8: 2007 Placebo Cutoffs for Private Schools